



LARGE-SCALE COSMIC ANOMALIES

Current Status, Future Prospects, and Possible Explanations

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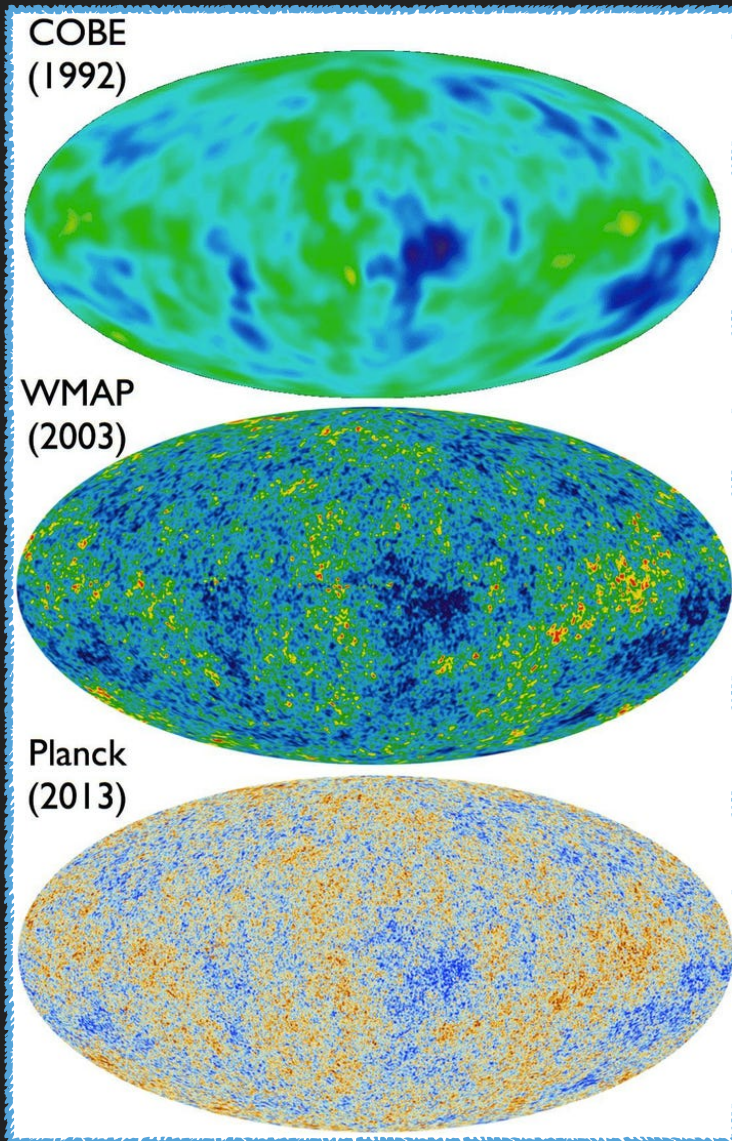
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COSMIC MICROWAVE BACKGROUND (CMB)



$$\Delta T = \sum_{\ell m} a_{\ell m} Y_{\ell m}(\theta, \phi)$$

Our standard model for the fluctuations (inflation):

- Sky is statistically isotropic
- $a_{\ell m}$ are independent Gaussian random variables

$$\langle a_{\ell m} a_{\ell' m'}^* \rangle = C_{\ell} \delta_{\ell \ell'} \delta_{m m'}$$

Angular Power Spectrum

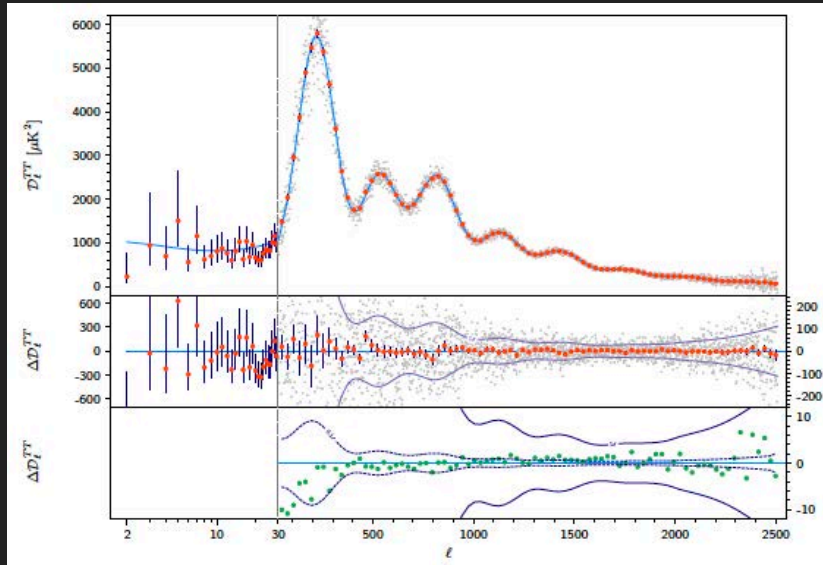
For full sky observations, **all** interesting information is contained in the estimator:

$$\hat{C}_{\ell} = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} |a_{\ell m}|^2$$

MEASURED ANGULAR POWER SPECTRA

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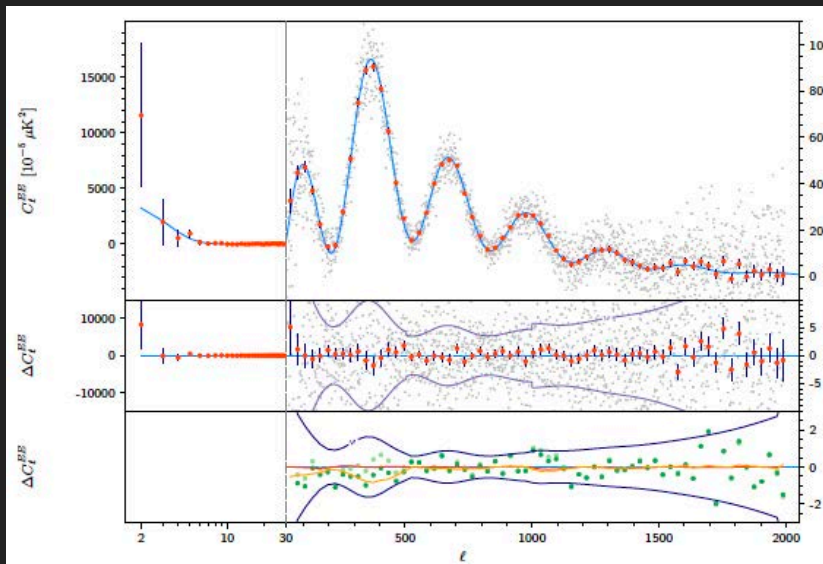
TT



6-parameter fit to $\gg 6$ points

- This is **ASTONISHING** experimental accomplishment.
- It shows **REMARKABLE** agreement with theory.

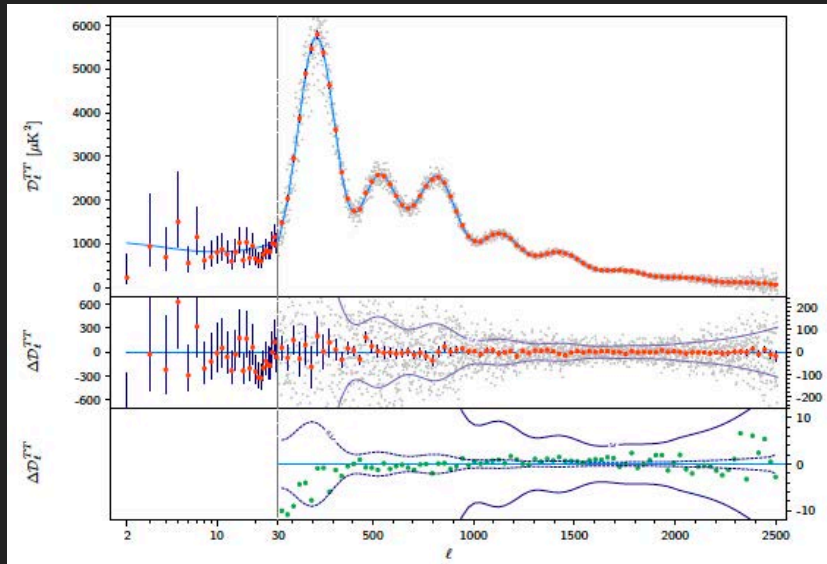
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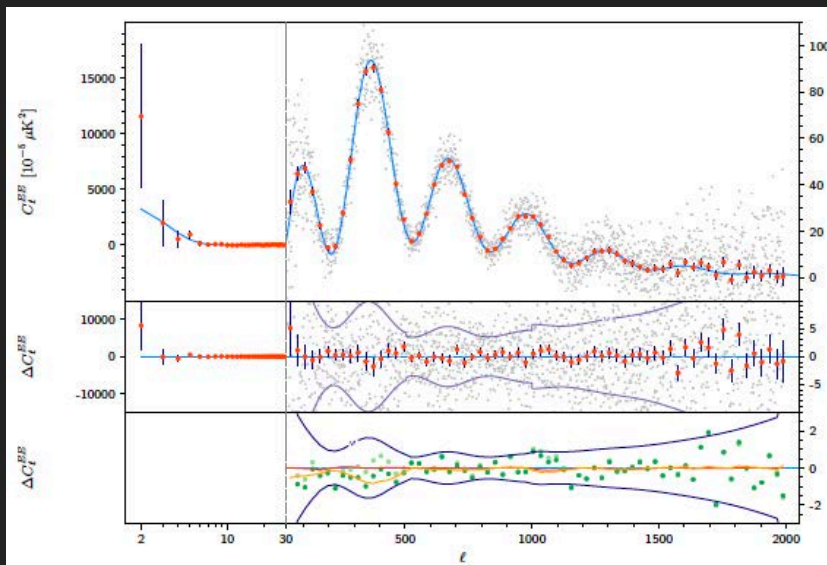
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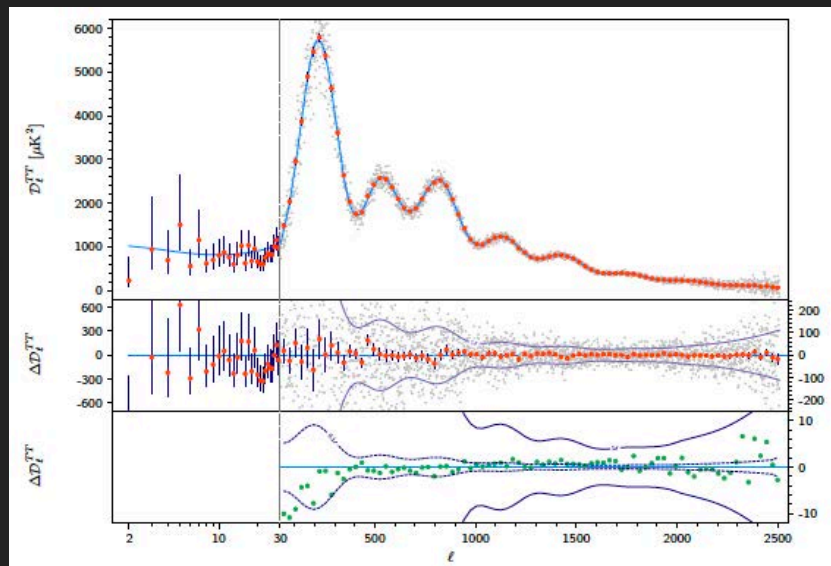
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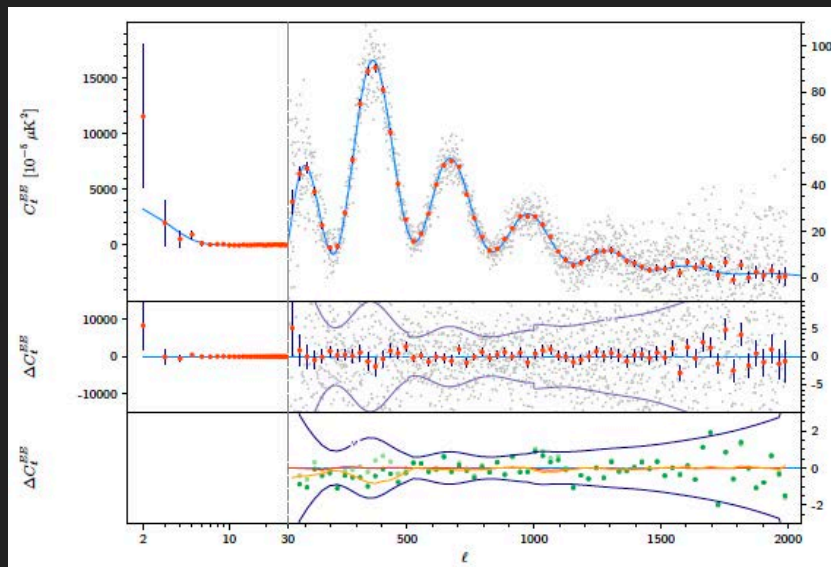
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Shouldn't we check these?

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Statistical isotropy of the CMB has been checked by different groups for both WMAP and Planck data.

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(Affiliations can be found after the references)

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Statistical isotropy of the CMB has been checked by different groups for both WMAP and Planck data.

Finding:

There are (large-scale) anomalous features that are unexpected or extremely unlikely in Λ CDM

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Special feature

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See:

E. Abdalla et al., JHEAp 34 (2022) 49–211

Schwarz, Copi, Huterer, Starkman, Class.Quant.Grav. 33 (2016) 18

In preparation:

Comprehensive and critical invited review for Physics Reports

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Almost everyone agrees now that these are real features on our CMB temperature sky and are not instrumental noise (as both WMAP and Planck found them) or foreground effects (as all component-separated maps found them).

Question:

Should we care? Are they hints of new physics?

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FOUR “REPRESENTATIVE” ANOMALY STATISTICS:

J. Jones, C. J. Copi, G. D. Starkman, Y. A. [arXiv:2310.12859]



$S_{1/2}$ — lack of large-angle correlations: $p \simeq 10^{-3}$

R_{Π} — odd-parity preference: $p \simeq 0.01-0.05$

σ^2_{16} — low northern variance: $p \simeq (2-4) \times 10^{-3}$

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1. Are they correlated in the tails of their pdfs?

2. What is their joint p-value?

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in Planck 2018 Commander, NILC, SEVEM, SMICA

1. Are they correlated in the tails of their pdfs?

2. What is their joint p-value?

- No cherry-picking or fine-tuning
- We took the statistics exactly as they were being used before

5 σ Evidence Against a Gaussian Random Statistically Isotropic Universe

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(Dated: May 29, 2025)

The standard cosmological model predicts statistically isotropic cosmic microwave background (CMB) fluctuations. However, several summary statistics of CMB isotropy have anomalous values, including: the low level of large-angle temperature correlations, $S_{1/2}$; the excess power in odd versus even low- ℓ multipoles, R^{TT} ; the (low) variance of large-scale temperature anisotropies in the ecliptic north, but not the south, σ_{16}^2 ; and the alignment and planarity of the quadrupole and octopole of temperature, S_{QO} . Individually, their low p -values are weak evidence for violation of statistical isotropy. We study the tail values of these statistics and find very little correlation among them. We show that the joint probability of all four anomalies occurring by chance in Λ CDM is likely $\leq 3 \times 10^{-8}$. We balance the impact of look-elsewhere effects and the existence of other anomalies on the significance of this result. We conclude that the anomalies should not be dismissed as flukes within Λ CDM.

jointly $> 5\sigma$ significant!

The sky appears NOT to be a typical realization of a Gaussian random statistically isotropic field.

J. Jones, C. J. Copi, G. D. Starkman, Y. A. [arXiv:2310.12859]

10⁸ realizations of CMB in best-fit Λ CDM

Stat.	Value	$S_{1/2}$	R^{TT}	σ_{16}^2	S_{QO}
Commander					
$S_{1/2}$	1272	1.5×10^{-3}	$\times 0.6$	$\times 27$	$\times 1.3$
R^{TT}	0.7896	2.8×10^{-5}	3.0×10^{-2}	$\times 1.1$	$\times 1.0$
σ_{16}^2	617.6	1.2×10^{-4}	1.0×10^{-4}	3.1×10^{-3}	$\times 1.7$
S_{QO}	0.7630	8.3×10^{-6}	1.3×10^{-4}	2.3×10^{-5}	4.4×10^{-3}
NILC					
$S_{1/2}$	1218	1.3×10^{-3}	$\times 0.4$	$\times 29$	$\times 1.3$
R^{TT}	0.7448	4.8×10^{-6}	1.0×10^{-2}	$\times 1.0$	$\times 1.0$
σ_{16}^2	605.9	9.2×10^{-5}	2.4×10^{-5}	2.5×10^{-3}	$\times 1.9$
S_{QO}	0.8203	6.3×10^{-7}	3.8×10^{-6}	1.8×10^{-6}	3.9×10^{-4}
SEVEM					
$S_{1/2}$	1215	1.3×10^{-3}	$\times 0.8$	$\times 33$	$\times 1.2$
R^{TT}	0.8194	5.6×10^{-5}	5.4×10^{-2}	$\times 1.2$	$\times 1.0$
σ_{16}^2	583.4	6.5×10^{-5}	1.0×10^{-4}	1.6×10^{-3}	$\times 1.5$
S_{QO}	0.6547	6.3×10^{-5}	2.2×10^{-3}	9.8×10^{-5}	4.1×10^{-2}
SMICA					
$S_{1/2}$	1257	1.4×10^{-3}	$\times 0.6$	$\times 25$	$\times 1.3$
R^{TT}	0.7906	2.8×10^{-5}	3.0×10^{-2}	$\times 1.1$	$\times 1.0$
σ_{16}^2	631.0	1.4×10^{-4}	1.3×10^{-4}	3.9×10^{-3}	$\times 1.8$
S_{QO}	0.8048	1.7×10^{-6}	2.9×10^{-5}	6.6×10^{-6}	9.2×10^{-4}

← pairwise correlations

triplet correlations



	$S_{1/2}$ and σ_{16}^2	S_{QO}
Commander		
$S_{1/2}$ and σ_{16}^2	1.2×10^{-4}	$\times 1.7$
S_{QO}	9.1×10^{-7}	4.4×10^{-3}
NILC		
$S_{1/2}$ and σ_{16}^2	9.2×10^{-5}	$\times 0.6$
S_{QO}	2.0×10^{-8}	3.9×10^{-4}
SEVEM		
$S_{1/2}$ and σ_{16}^2	6.5×10^{-5}	$\times 1.3$
S_{QO}	3.6×10^{-6}	4.1×10^{-2}
SMICA		
$S_{1/2}$ and σ_{16}^2	1.4×10^{-4}	$\times 2.1$
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Are the anomalies correlated in Λ CDM?

Map	p_4	Correlation Factor
Commander	3×10^{-8}	51
NILC	$< 1 \times 10^{-8}$	N/A
SEVEM	18×10^{-8}	40
SMICA	1×10^{-8}	64

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Our conclusion:

**A Gaussian random statistically isotropic universe
is falsified at $>5\sigma$ in CMB TT correlations!**

DISCUSS:

1. You can't believe data without a **model**, i.e., you can't falsify a model without an alternative
2. **Look-elsewhere** penalties, i.e., you can always find anomalous statistics

The typical justification of a 5σ threshold for discovery is that it overwhelms even strong look-elsewhere concerns.

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Look-elsewhere penalties vs. look-more-closely rewards

$S_{1/2}$ — lack of large-angle correlations, $p \approx 10^{-3}$

Look elsewhere:

- why 60° ? why 180° ? why $C(\theta)^2$? why $d\cos\theta$?

Look more closely:

- $p(S_{1/2}^{EE}) \sim 10^{-3}$ [Chiocchetta et al., JCAP 08 (2021) 015]

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R_Π – odd-parity preference, $p \approx 0.01-0.05$

Look elsewhere:

- why $\ell_{\max}=27$? why odd > even not even > odd

Look more closely:

- first 9 consecutive pairs $C_{2\ell+1} > C_{2\ell}$, $\ell=1, \dots, 9$; estimate $p \sim 2 \times 2^{-9} \approx 0.004$ (w. look-elsewhere)

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- why N? why ecliptic? why $N_{\text{side}}=16$?

Look more closely: [Planck 2013 Isotropy and Statistics]

- ecliptic not optimum, galactic also ~ 0.003
- $p(\text{low (north) skewness}, N_{\text{side}}=32) = 0.02-0.03$
- $p(\text{high kurtosis}, N_{\text{side}}=32) = 0.03$

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Look elsewhere:

- ??

Look more closely:

- “axis of evil” $\ell=2-5$ [Land & Magueijo PRL95 (2005) 071301]
- “uncanny correlation of azimuthal phases between $\ell=3$ & $\ell=5$. (ibid.)
- oriented areas $\ell=2-8$ inconsistent at 0.2% [Copi, Huterer, Starkman PRD 70 (2004) 043515]

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While the cosmic orchestra may be playing the Λ CDM symphony, somebody gave the bass and tuba the wrong score.

They're trying very hard to keep quiet about it.

But we must demand an explanation.

WITH SO MANY ANOMALIES, WHAT DO WE DO?

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Physics explanations:

1. These are statistical flukes in standard Λ CDM
2. These are not statistical flukes

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Physics explanations:

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2. These are not statistical flukes

Making progress:

1. Test the “**fluke** hypothesis” (i.e. test Λ CDM!)
 - **Philosophy**: assume Λ CDM is correct and see how the measured anomalies affect predictions for other observables (like CMB polarization, large-scale structure, etc).
2. Make reasonable **phenomenological extrapolations** and test them.
 - **Philosophy**: assume each anomaly is “physical” and guess what that implies for other observables
3. Find a **fundamental physics model**, make testable predictions.

FUNDAMENTAL PHYSICS MODELS TO EXPLAIN CMB ANOMALIES

Requirements:

1. Break statistical isotropy

⇒ Generate nonzero off-diagonal elements in harmonic-space 2-point correlations

2. Affect scales that were causally disconnected until recently

$$C_{\ell m \ell' m'} \equiv \langle a_{\ell m} a_{\ell' m'}^* \rangle$$

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Our best bet: change of boundary conditions

⇒ cosmic topology



FUNDAMENTAL PHYSICS MODELS TO EXPLAIN CMB ANOMALIES

Requirements:

COMPACT Collaboration, JCAP 03 (2024) 036

Symbol	Name	Compact Dimensions	Orientable	Homogeneous	Isotropic
E_1	3-torus	3	Yes	Yes	No
E_2	Half-turn	3	Yes	No	No
E_3	Quarter-turn	3	Yes	No	No
E_4	Third-turn	3	Yes	No	No
E_5	Sixth-turn	3	Yes	No	No
E_6	Hantzsche-Wendt	3	Yes	No	No
E_7	Klein space	3	No	No	No
E_8	— (horizontal flip)	3	No	No	No
E_9	— (vertical flip)	3	No	No	No
E_{10}	— (half-turn)	3	No	No	No
E_{11}	Chimney space	2	Yes	Yes	No
E_{12}	— (half-turn)	2	Yes	No	No
E_{13}	— (vertical flip)	2	No	No	No
E_{14}	— (horizontal flip)	2	No	No	No
E_{15}	— (half-turn + flip)	2	No	No	No
$E_{16}^{(h)}$	Slab (unrotated)	1	Yes	Yes	No
$E_{16}^{(i)}$	Slab (rotated)	1	Yes	No	No
E_{17}	Slab (flip)	1	No	No	No
E_{18}	Covering space	0	Yes	Yes	Yes

It is
Our

m'

FUNDAMENTAL PHYSICS MODELS TO EXPLAIN CMB ANOMALIES

Requirements:

1. Break statistical isotropy
 $\Rightarrow$ Generate nonzero off-diagonal elements in harmonic-space 2-point correlations

2. Affect scales that were causally disconnected until recently

$$C_{\ell m \ell' m'} \equiv \langle a_{\ell m} a_{\ell' m'}^* \rangle$$

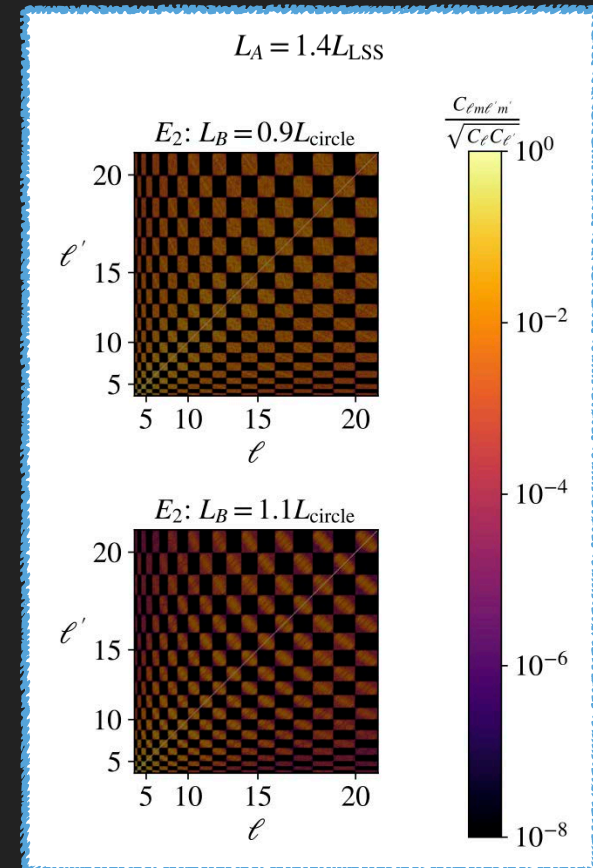
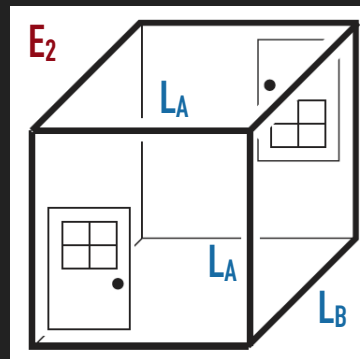
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AN EXAMPLE:





COMPACT

[international theoretical collaboration founded by me and Glenn Starkman in 2022]

Collaboration for **O**bservations, **M**odels and **P**redictions of **A**nomalies and **C**osmic **T**opology

A 10-year program to use all cosmological data (CMB, LSS, 21cm) to understand cosmic anomalies, and to discover the topology of the Universe.

(Or demonstrate conclusively that discovering it is beyond our reach for the foreseeable future.)

A highly ambitious plan
(currently funded by NASA)



Yashar AKRAMI



Craia COPI



Andrew JAFFE



Arthur KOSOWSKY



Thiago PEREIRA



Glenn STARKMAN



Stefano ANSELM



Fernando CORNET-GOMEZ



Javier DUQUE



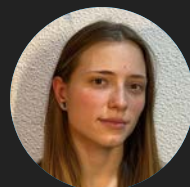
Devan MIHAYLOV



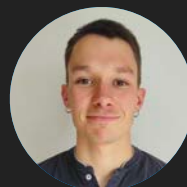
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Ananda SMITH



Johannes ESKILT



Valeri VARDANYAN



Pip PETERSEN



Samanta SAHA



Quinn TAYLOR

PHYSICAL REVIEW LETTERS 132, 171501 (2024)

Featured in Physics

Goals
Motivations
Search strategies

Promise of Future Searches for Cosmic Topology

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The shortest distance around the Universe through us is unlikely to be much larger than the horizon diameter if microwave background anomalies are due to cosmic topology. We show that observational constraints from the lack of matched temperature circles in the microwave background leave many possibilities for such topologies. We evaluate the detectability of microwave background multipole correlations for sample cases. Searches for topology signatures in observational data over the large space of possible topologies pose a formidable computational challenge.

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COMPACT Collaboration (Y. A. et al.), Phys. Rev. Lett. 132 (2024) 17

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CONCLUSIONS

There are (large-scale) anomalous features in the CMB temperature sky that are unexpected or extremely unlikely in Λ CDM.

These cosmic anomalies are real and are not instrumental noise or foreground effects.

Their significance is 2.5σ – 4σ individually, but their joint significance in the tails of their distributions is $> 5\sigma$.

The typical justification of a 5σ threshold for discovery is that it overwhelms even strong look-elsewhere concerns.

Almost all of them imply violation of statistical isotropy.

One can/should study them further by testing the standard Λ CDM model, making phenomenological extrapolations, and finding fundamental physics models.

We need to study CMB polarization data, as well as other cosmological observables (LSS, 21cm, etc), to shed light on the nature of anomalies.

We should continue studying the anomalies and try to find more.